

# Quick determination of the manufacturing performance of a direct-fired industrial furnace using an implicitly solved, multiple 1D approach

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# Agenda

**Objective & General Idea**

**Geometrical & Mathematical  
Discretization**

**Boundary Conditions &  
Results**

**Outlook**

# Objective & General idea

## Objective:

Reduce the computational time and the required computational power to estimate the average temperature distribution within an industrial furnace

## Expected Benefits:

- Better understanding of heat transfer within furnace without measurement equipment  
→ Digital sensor
- Better knowledge of fuel/ power consumption when changing operating conditions for new products  
→ Initial parametrization
- Estimation of product properties using temperature- property relationships

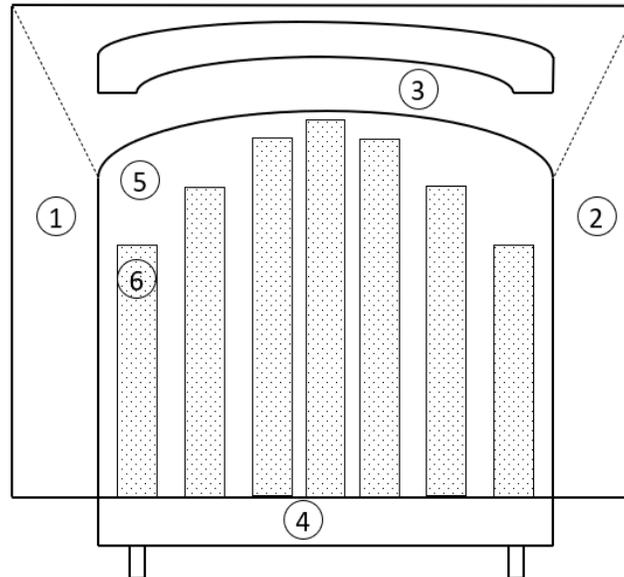
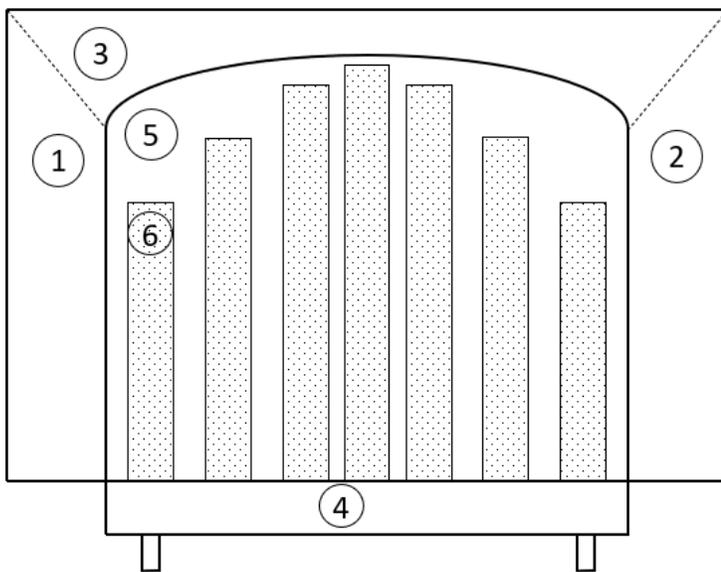


**How to implement this?**

# Objective and General Idea

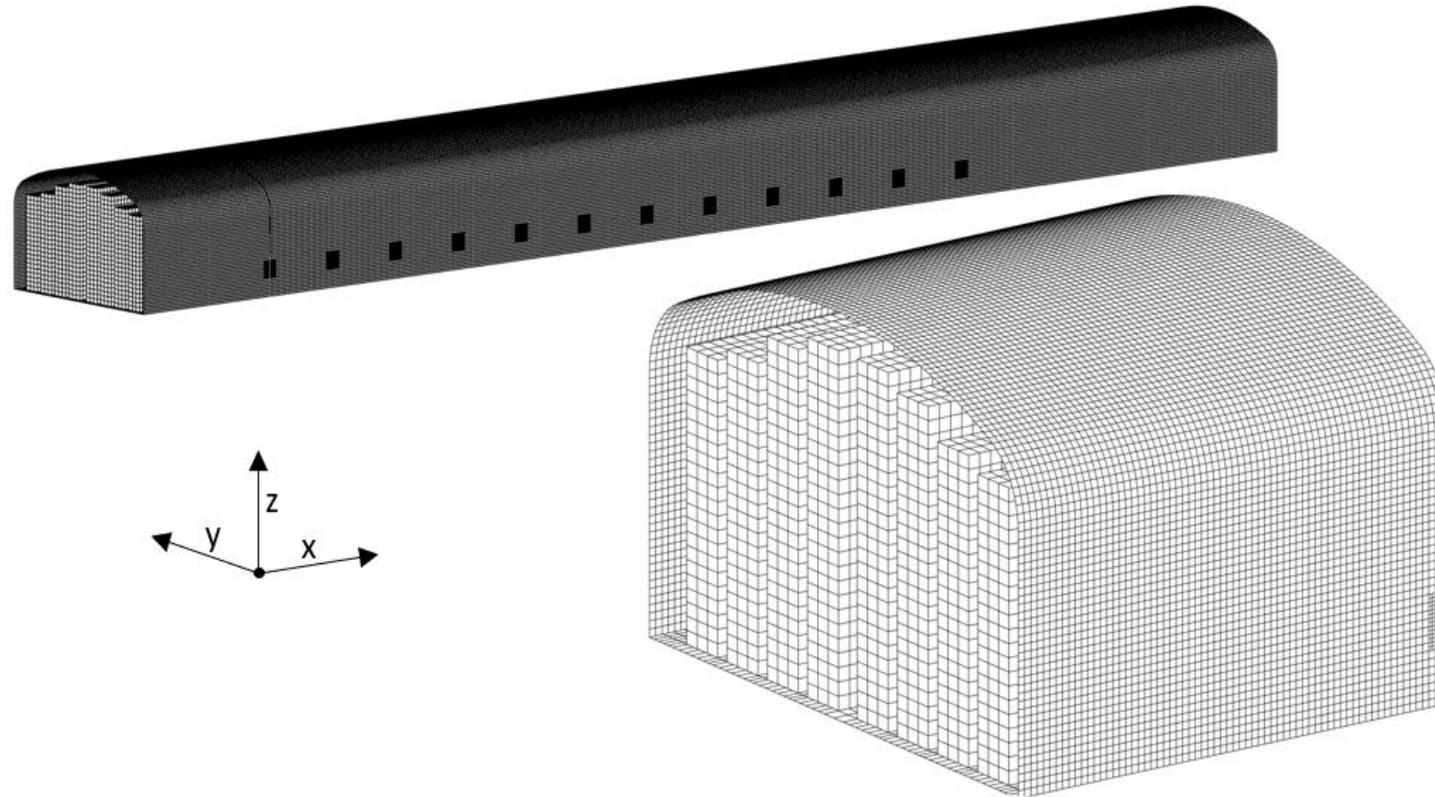
**Idea:** Simplified subdivision of geometrical domain into separate one-dimensional zones

**Example:** Tunnelfurnace producing stacked refractory bricks



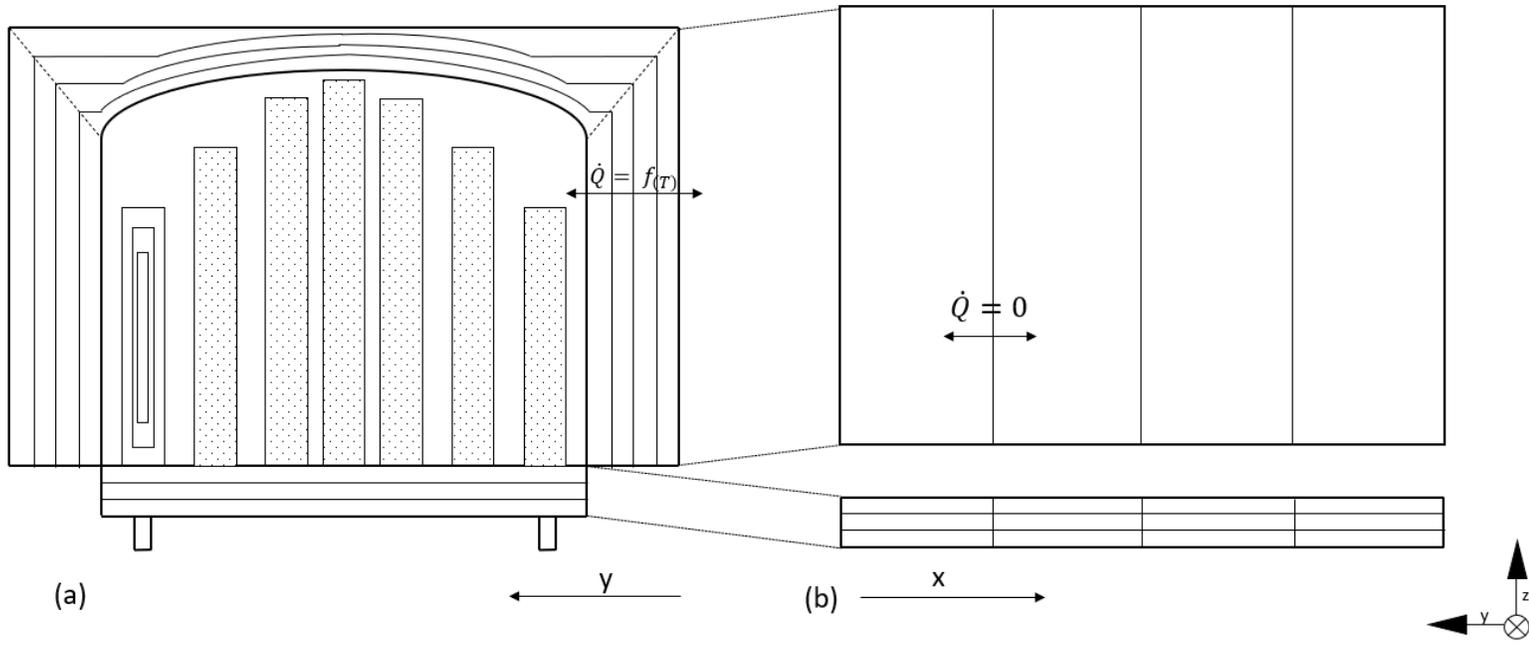
- 1 & 2: side wall segments
- 3: ceiling segments
- 4: kiln cart platform
- 5: atmosphere segments
- 6: product stacks

# Geometrical & Mathematical Discretization



Observed simulation geometry of furnace inside surfaces and product outside surfaces

# Geometrical & Mathematical Discretization



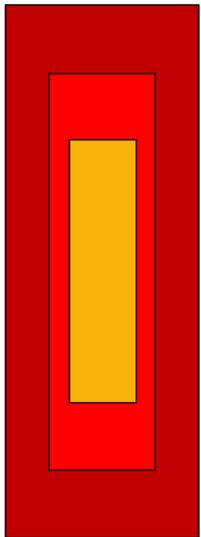
- a) Furnace cross- section discretization layers
- b) Side wall and kiln cart platform discretization layers

Heat can only be transferred along the respective one- dimensional zone and exchanged between different zones

# Geometrical & Mathematical Discretization

Discretization possibilities:

→ What represents reality best?

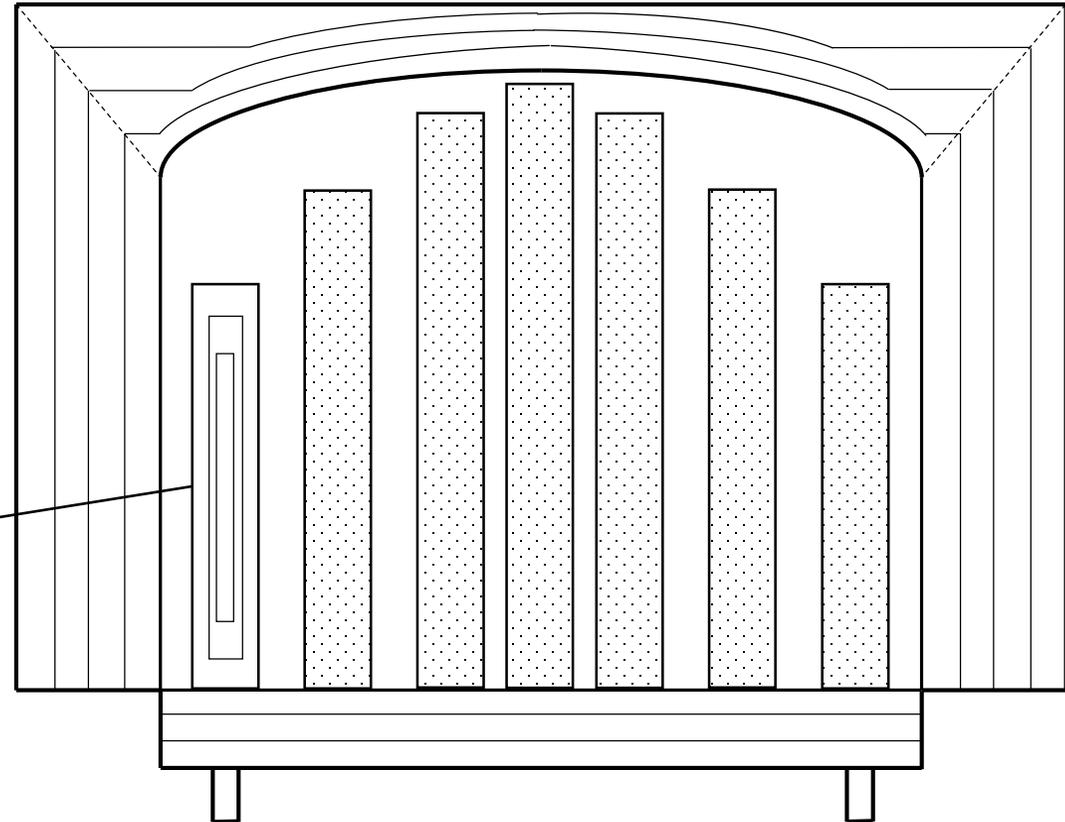


(a)



(b)

- a) Concentric discretization
- b) Linear discretization



Concentric representation in this case better because of low thermal conductivity of product material and stack measurements

# Geometrical & Mathematical Discretization

$$ld T_{i-1}^{n+1} + md T_i^{n+1} + ud T_{i+1}^{n+1} + rad T_j^{n+1} + rad_2 T_k^{n+1} = RHS$$

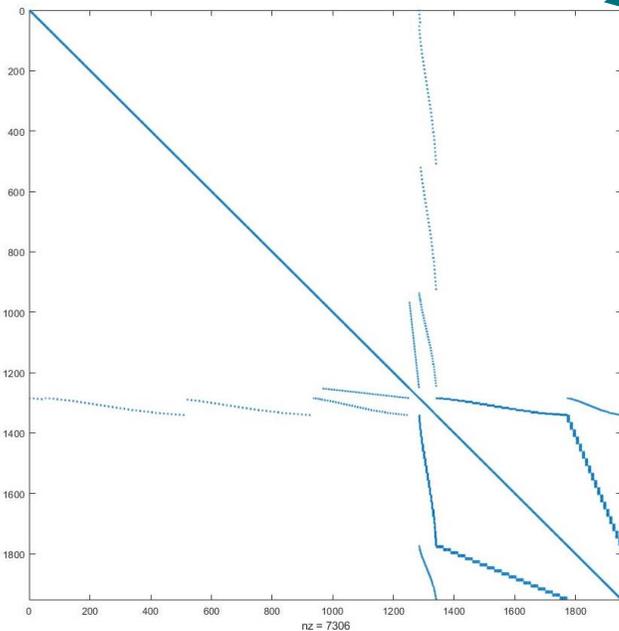


$$AT = RHS$$

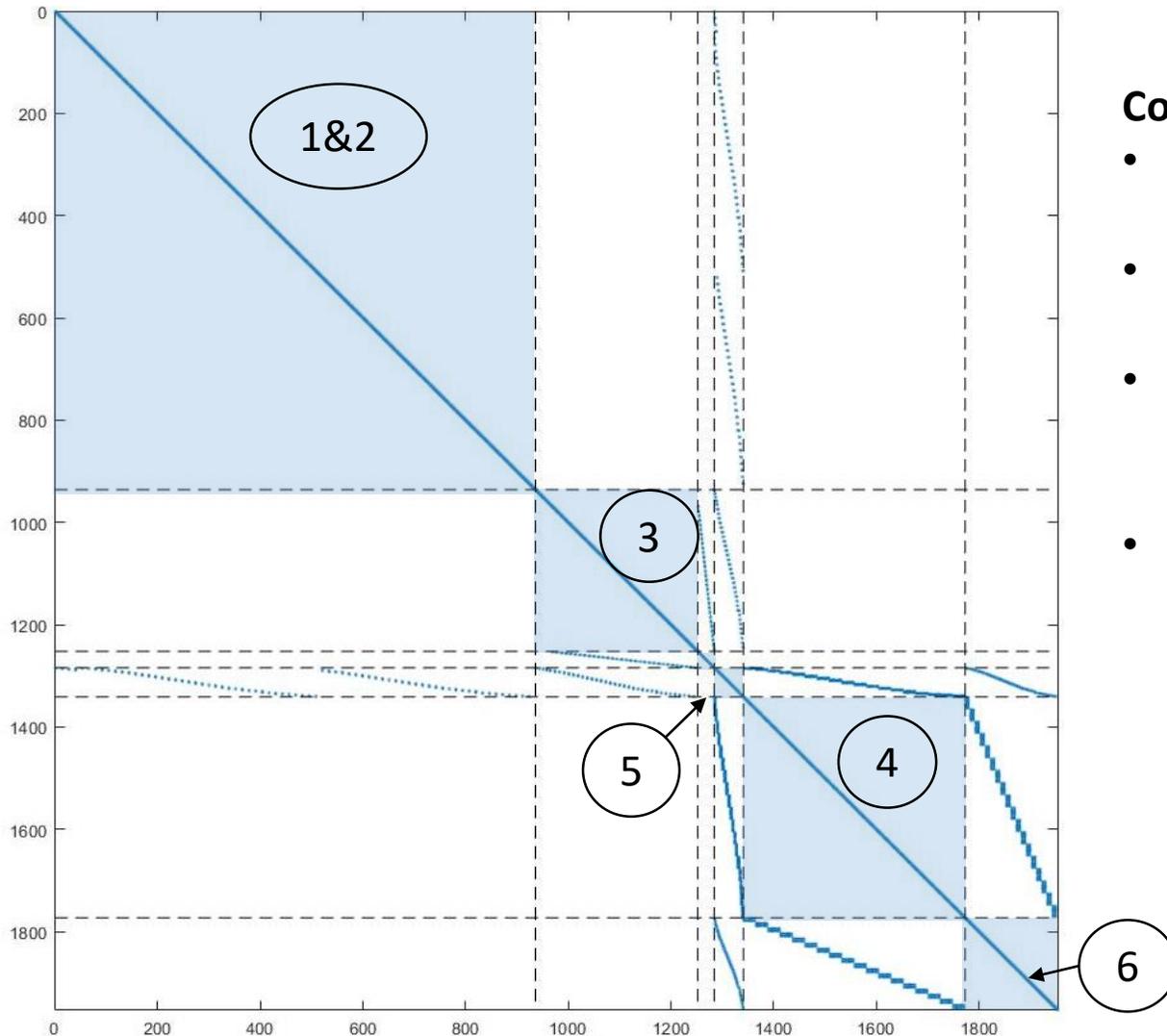
$$\begin{bmatrix} T_{RB1} \\ T_{RB2} \\ T_{RB3} \\ T_1 \\ T_2 \\ \vdots \\ \vdots \\ T_{1919} \end{bmatrix}$$

=

$$\begin{bmatrix} 1 \\ 1 \\ 1 \\ \text{sourceterm}_1 + \text{accumulationterm}_1 + \text{radiationterms}_1 \\ \text{sourceterm}_2 + \text{accumulationterm}_2 + \text{radiationterms}_2 \\ \vdots \\ \vdots \\ \text{sourceterms}_{1919} + \text{accumulationterms}_{1919} + \text{radiationterms}_{1919} \end{bmatrix}$$

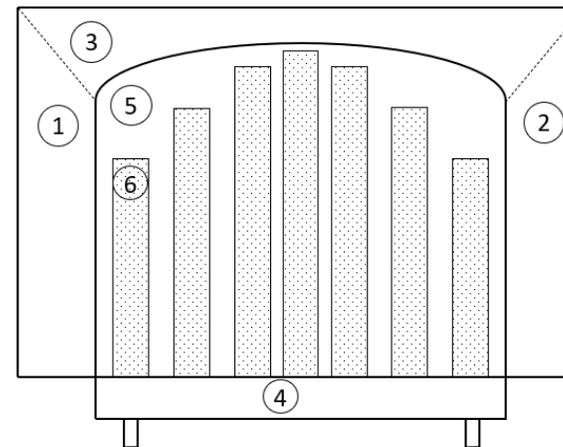


# Geometrical & Mathematical Discretization



## Coefficient Matrix:

- Indicates connectivity between each cell
  - Describes which cell can transfer heat to another cell
- Radiation terms are placed explicitly on RHS, thus no communication between zones 1&2 and zones 6 are visible
- Coefficient matrix is dynamic
  - Different Stack patterns possible, resulting in a variation of cell amount
- Source terms are placed explicitly on RHS



# Geometrical & Mathematical Discretization

## Surface to Surface model:

- Radiation is a surface phenomenon and depends on how the surfaces are exposed to each other  
→ Participating media are neglected

1) Energy Flux leaving a surface can be expressed as:

$$q_{out_i} = \varepsilon_i \sigma T_i^4 + \rho_i \sum_{j=1}^N F_{ji} q_{out_j} \quad \equiv \quad J_i = E_i + (1 - \varepsilon_i) \sum_{j=1}^N F_{ji} J_j$$

2) This can be expressed in matrix form:

$$KJ = E$$

$$K = \begin{bmatrix} 1 & (\varepsilon_1 - 1)F_{12} & (\varepsilon_1 - 1)F_{13} & (\varepsilon_1 - 1)F_{14} & (\varepsilon_1 - 1)F_{15} & \dots \\ (\varepsilon_2 - 1)F_{21} & 1 & (\varepsilon_2 - 1)F_{23} & (\varepsilon_2 - 1)F_{24} & (\varepsilon_2 - 1)F_{25} & \dots \\ \vdots & \vdots & \vdots & \vdots & \vdots & \ddots \end{bmatrix} \quad J = \begin{bmatrix} q_1 \\ q_2 \\ \vdots \end{bmatrix} \quad E = \begin{bmatrix} \varepsilon_1 \sigma T_1^4 \\ \varepsilon_2 \sigma T_2^4 \\ \vdots \end{bmatrix}$$

**J corresponds to the flux leaving the surface → net flux of surface can be computed**

# Geometrical & Mathematical Discretization

## Computation of view factor

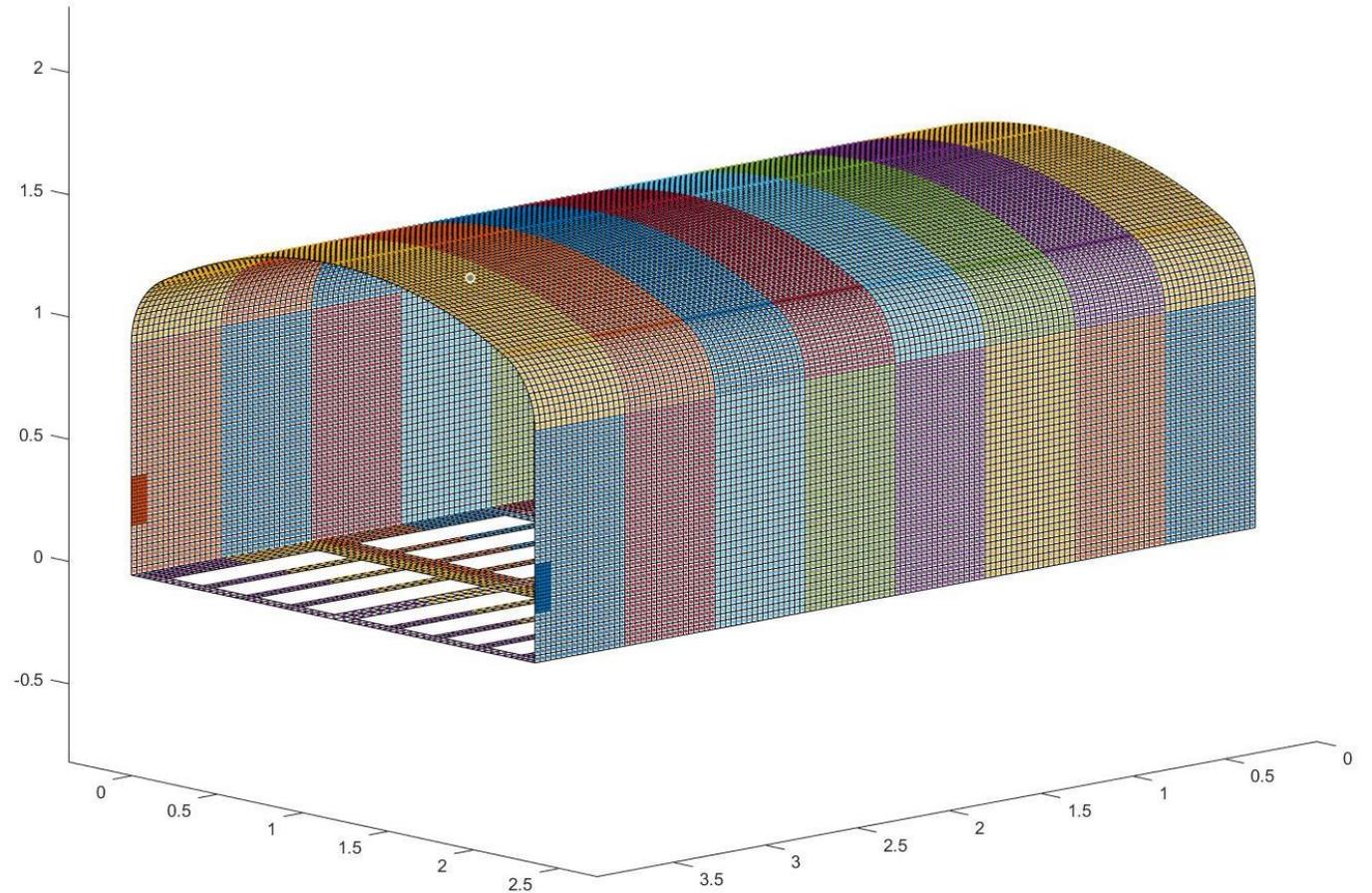
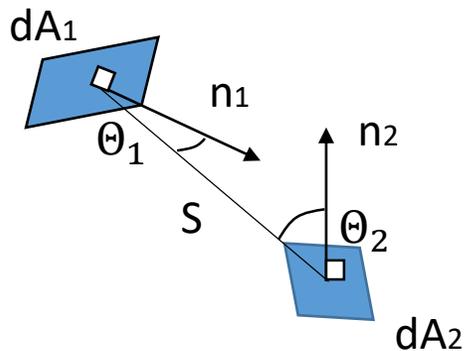
Macroscopic surfaces:

→ Corresponds to simulation cell size

Microscopic surfaces:

→ Required to pre- compute view factors  
via numerical integration

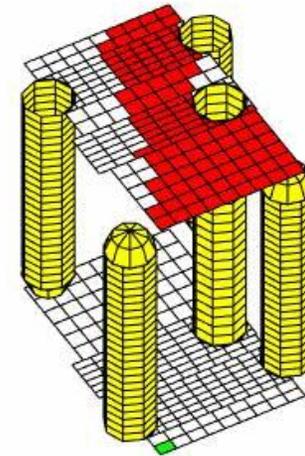
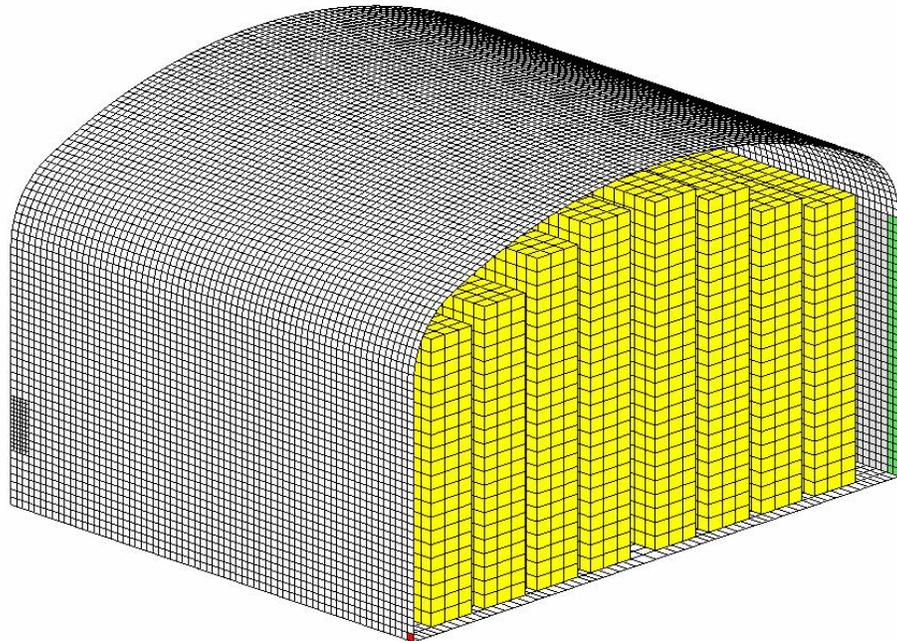
$$dF_{ij} = \frac{1}{A_i} \int_{dA_1} \int_{dA_2} \frac{\cos \Theta_1 \cos \Theta_2}{\pi S^2} \delta_{12} dA_1 dA_2$$



# Geometrical & Mathematical Discretization

## Computation of view factor

- Changing geometry if stack pattern of product changes
  - Re- computation of view factor matrix required
- One matrix for each geometry required
  - Highly time- consuming if performed on complete furnace
  - Separation into representative regions and perform sub- computations
  - While simulation runs, assembling of these regions into the current valid matrix



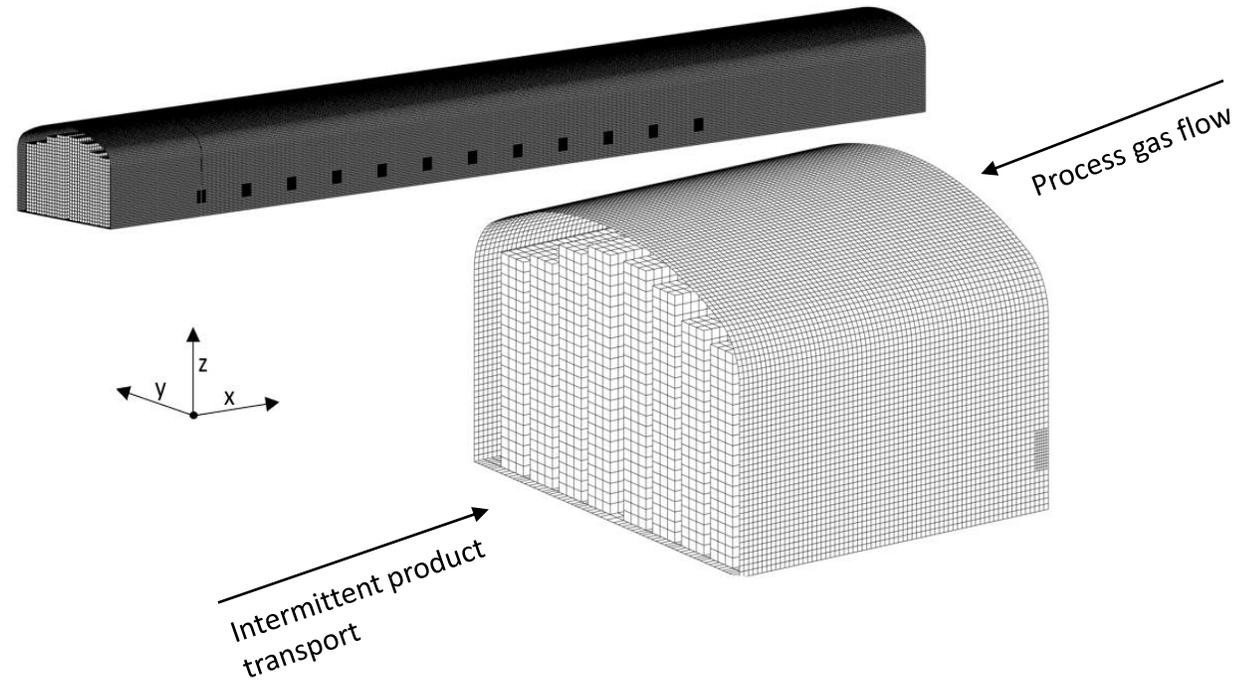
# Boundary Conditions & Results

## Geometry Specifications:

- Length of furnace: 15.687 m
- Width of furnace: 2.35 m → Only burning zone simulated
- Height of furnace: ~ 1.5 m

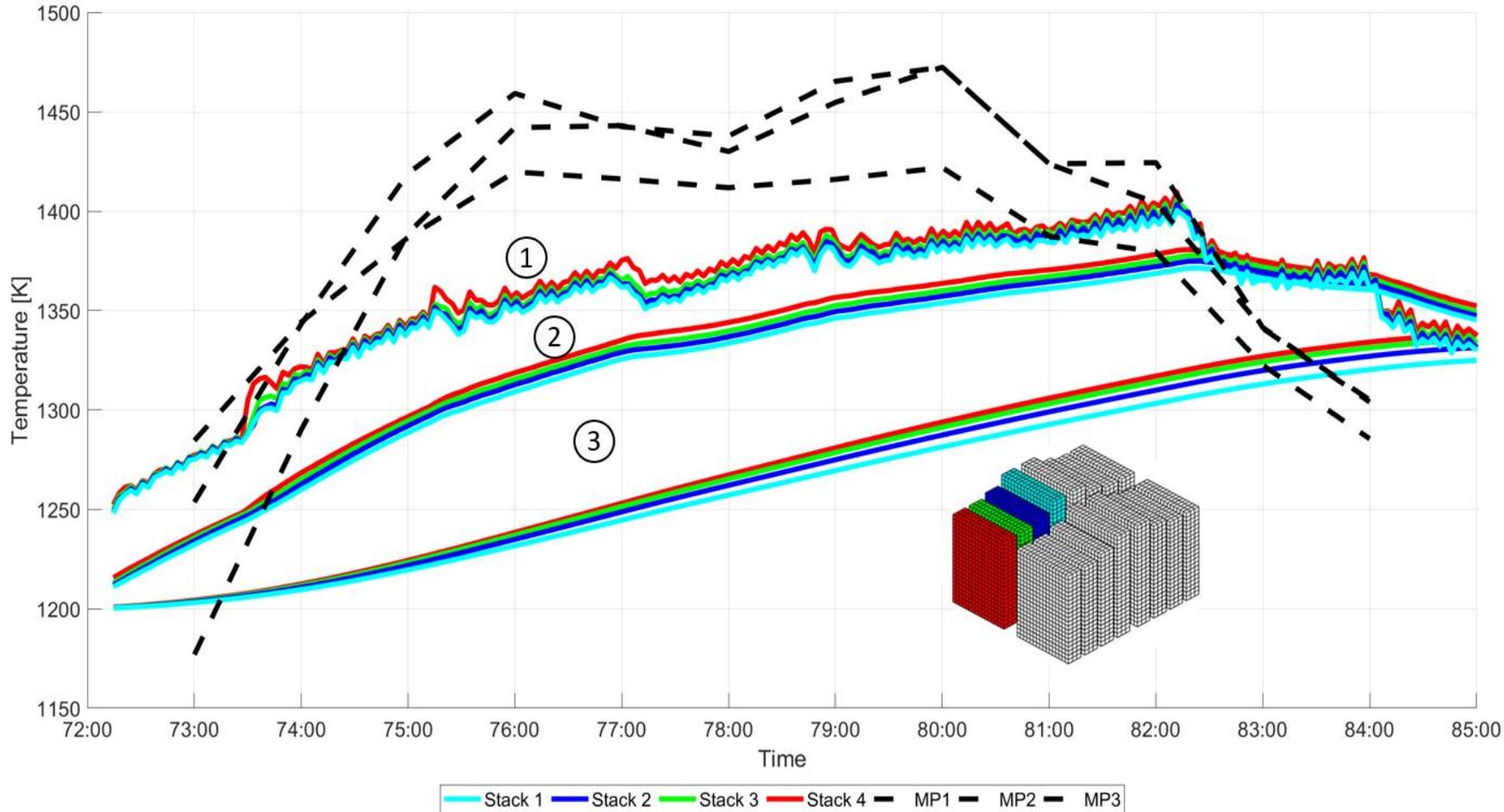
## Initial Conditions:

- Counter- current process gas stream
- $T_{\text{init}}$  of counter- current stream: 1300 K
- $\dot{m}$  of counter current stream: 0.1 kg/s
- Number of burner Pairs: 12
- Average power per burner: 85 kW – 205 kW
- Air number of burner: ~ 0.7 – 0.8
- Initial temperature of product stacks, kiln cart: ~1200 K
- Product dwell time: 105 min



# Boundary Conditions & Results

## Temperature profile of tracked kiln cart



--- measurement data at various product stack surface locations

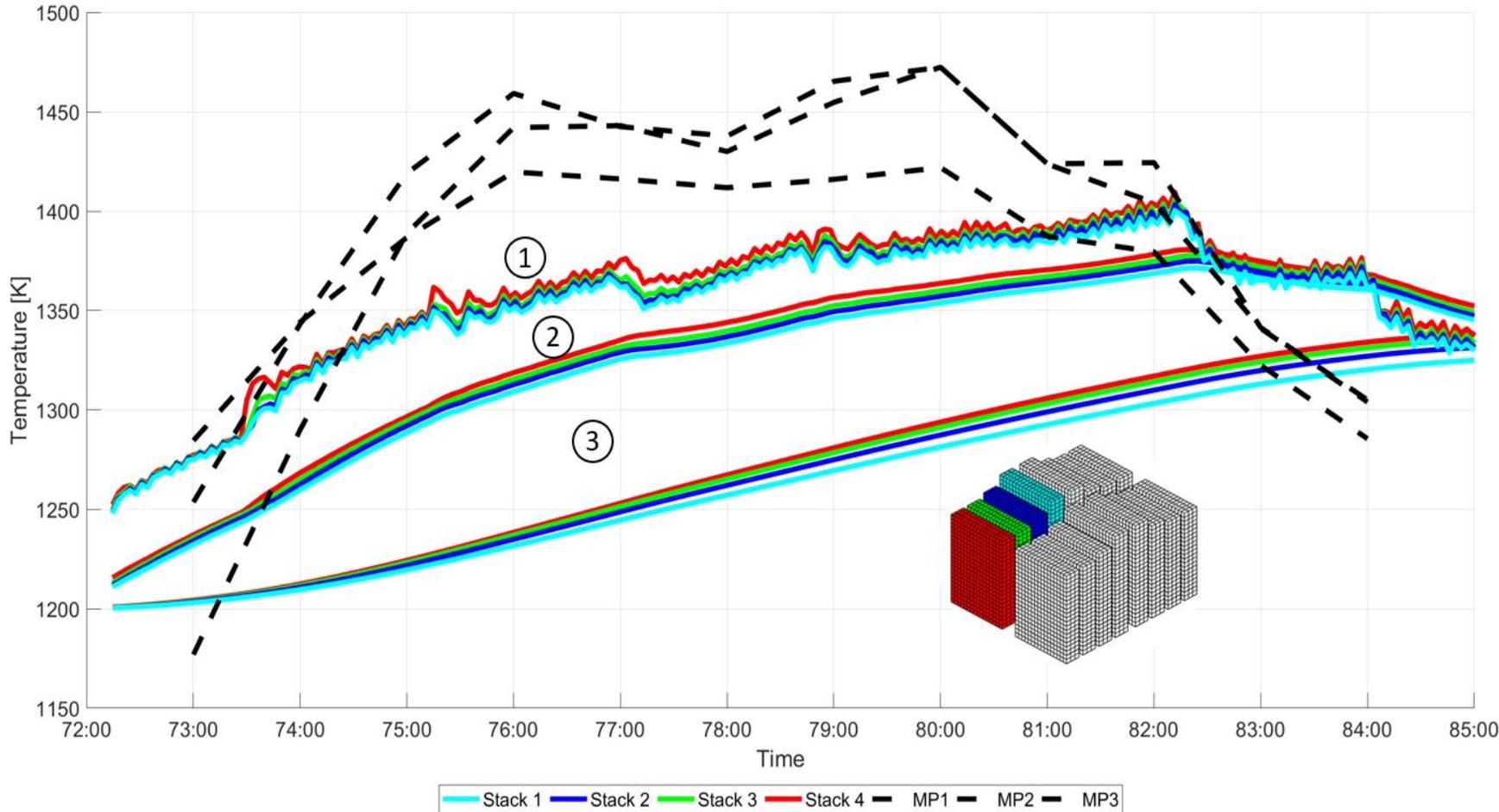
### Simulation

- ① Average surface temperature
- ⋮
- ⋮
- ⋮
- ③ Average core temperature

Simulated production time of 85 hours within of 340 seconds of computational time

# Boundary Conditions & Results

Direct comparison only between dashed lines and 1 possible!



→ Difference in temperature gradients

## Possible Causes:

- Radiation Model (S2S)
- Secondary Reactions (excess air)
- Underestimation of heat transfer coefficient

# Outlook

- Analysis of heat transfer coefficient and dwell time
  - Conduction of several simulations to evaluate impact on temperature profile
- Detailed measurement campaigns
  - Increase confidence in data
  - Yield data for analysis of secondary reactions
- Inclusion of secondary reactions
  - Excess air due to not airtight furnace
  - Sub- stoichiometric combustion provides fuel
  - Reaction between excess air and remaining fuel cause secondary source terms, which increases temperature gradient on the product inlet side

**Thank you for your attention**